

Supplementary material for the work: “Path Integral Monte Carlo on a Sphere”

Riccardo Fantoni*

Università di Trieste, Dipartimento di Fisica, strada Costiera 11, 34151 Grignano (Trieste), Italy

(Dated: August 21, 2026)

Supplementary material to the article “Path Integral Monte Carlo on a Sphere”.

Keywords: Path Integral; Monte Carlo; Sphere; Quantum Fluid; Bosons; Fermions; Anyons; Thermodynamics; Structure; Superfluidity; Sign Problem

I. INTRODUCTION

We here report the FORTRAN code listing of the code used in the simulations developed in the publication “Path Integral Monte Carlo on a Sphere”. This is shown in Appendix A. The model studied in that publication was that of a many body fluid of N particles at $\mathbf{r}_i$, $i = 1, 2, \dots, N$, on a sphere of radius a . Where $\mathbf{r} = (\theta, \varphi)$ with $\theta \in]-\pi/2, \pi/2]$ the polar angle and $\varphi \in]-\pi, \pi]$ the azimuthal angle. The metric of the sphere is $ds^2 = g_{\mu\nu} dr^\mu dr^\nu$ with a diagonal metric tensor $g_{\mu\nu}$ such that $g_{11} = a^2$ and $g_{22} = a^2 \cos^2 \theta$.

The plane waves ¹ Path Integral Monte Carlo (PIMC) method used in our computer experiments is the one described in Ref. [2]. A single MC step is made of the exchange of a randomly chosen pair of particles through the *Lévy construction* of two Brownian bridges between two randomly chosen timeslices on different particles paths (see Section V.G of Ref. [2] and references therein for the multislice move) and of a displacement of all the timeslices of a particle path chosen at random (the singleslice move). The exchange move allows to sample the permutation sum necessary in the calculation of the symmetric Bose-Einstein density matrix. The extent of the singleslice displacement is chosen at the beginning of the run through the input variable **ALPHA** or it can be adjusted during the run every **IRATIO** MC steps so to have acceptance ratios closest to 1/2 (this functionality is commented out in the present listing).

We discretize the imaginary time between 0 and **BETA** into **FTN0** timeslices of length $\tau = \text{LS} = \text{BETA}/\text{FTN0}$. One usually wants to compare simulations at fixed **LS**. The multislice move requires the reconstruction of a randomly chosen number $\text{MBM} \leq \text{MBMM} \leq \text{FNT0}$ of timeslices between a randomly chosen timeslice **CP** on a randomly chosen particle **IP** and a timeslice on a randomly chosen particle **KP**. Here **MBMM** is the maximum number of timeslices in a Brownian bridge. The singleslice move requires the displacement of all the **FTN0** timeslices of the path of the particle **IP** chosen at random. So a single MC **STEP** requires a maximum of $2\text{MBMM} + \text{FTN0}$ timeslice moves. In the code we wrote the FORTRAN instructions for the multislice

move in lowercase and the ones for the singleslice move in uppercase. The simulation sets **KP=IP** in the exchange move if the logical variable **IFB** is set to **FALSE**. So that if it is set to **TRUE** Bose-Einstein statistics is used, otherwise is used Boltzmann statistics. The simulation uses only the multislice move if the logical variable **IFBRIDGE** is **TRUE** and only the singleslice move if the logical variable **IFDISP** is **TRUE**. The simulation lasts for a total number of MC steps **NSTEP**. All this variables can be chosen in the **data-gr-rs.in** simulation configuration input file at startup.

On a sphere it is necessary to choose **DIM= 2** with a number of particles $N = \text{NP}$ of mass **FTM** with natural units $\hbar = k_B = 1$. One has to specify also the radius of the sphere **RADIUS** and the absolute temperature **TEMP**.

The pair potential between the particles **POTK** is encoded in **SUBROUTINE POT** at the end of the code listing. It includes the Coulomb potential that can be chosen by setting the string **POTK** equal to **COULOMB**. The ideal gas is obtained choosing the string **FREE**. This can be set up in the **data-gr-rs.in** simulation configuration input file. The variables **RCUT**, **SIG**, **EPSR**, **EPSA**, and **EPS** in the simulation configuration input file are used to specify other properties of a non Coulomb pair potential.

The simulation calculates both thermodynamic quantities and static structural properties. For the thermodynamic quantities we measure: the kinetic energy **KE**, the physical potential energy **V**, the geometric effective potential energy $\mathbf{W} = -\sum_{i=1}^N \ln \sqrt{g(\mathbf{r}_i)}/\tau$ where g is the determinant of the sphere metric tensor, and the superfluid fraction **SF**. These quantities are stored in the output file **fort.9** every **IPRINT** MC steps. Whereas the path configurations output file **CNFILE** is stored in a *.xyz* format every **ISAVE** MC steps. The first **IEQUI** MC steps are used for the equilibration of the Markov chain. Quantities are only calculated after these equilibration steps. For the structural properties we measure the radial distribution function $g(r)$, with r the Euclidean distance, which is written in the output file **rdf.dat**. In the current implementation of the code, the $g(r)$ is only calculated during the displacement move every **ICALCG** timeslices.

If the variable **INIT** is set to 0 the simulation starts from a path with all particles at all timeslices on the equator $\theta = 0$ at $\varphi = 0$, if it is set to 1 it starts from a path with the particles randomly distributed uniformly on the equator with all timeslices copied above the first

* riccardo.fantoni@scuola.istruzione.it

¹ For a coherent states PIMC see Ref. [1].

one for each particle, if it is set to 2 it reads the paths configuration from the file `CNFILE` stored on disk, if it is set to 3 it does a complete restart from the file `CNFILE` and the frozen configuration `back.dat` both stored on disk.

The variable `SEED`, set in the simulation configuration input file, is the positive integer seed of the pseudo random number generator.

For the RPIMC algorithm also used in the work for the simulations of fermions [3, 4] and anyons we modified the code presented here as described in the main text of the article.

ACKNOWLEDGMENTS

I would like to thank prof. Saverio Moroni for his support in the development of the brownian bridge and the consequent particles permutation sampling.

Appendix A: The code

This is the code used for the PIMC computer experiment. We list here the main FORTRAN code `pimc-sph-rs.f` with the included `mc-sph.par` parameters file. And the input simulation configuration file `data-gr-rs.in` that is read at the beginning of the run.

```
*****
*** pimc-sph-rs.f *****
*****

      PROGRAM PIMC
      IMPLICIT NONE
C *****
C ** MONTE CARLO SIMULATION PROGRAM FOR [PW] PATH INTEGRAL **
C **
C ** on a sphere of radius RADIUS **
C **
C ** space dimensions: DIM=2 **
C ** number of particles: NP **
C ** number of timesteps: FTNO **
C ** units: hbar=k_B=1 **
C ** BETA=1/TEMP=FTNO*LS (LS imaginary time spacing) **
C **
C ** OBSERVABLES: **
C ** kinetic energy KE **
C ** potential energy V **
C ** forces virial W **
C ** superfluid fraction SF **
C ** radial distribution function on 'rdf.dat' **
C *****
      INCLUDE 'mc-sph.par' ! parameters

      INTEGER*4 SEED
      INTEGER*8 IDIM, STEP, I, J, K
      INTEGER*8 C1, CP, IP, KP, NIP, NKP, LL, OUT1, OUT2, PIP
      INTEGER*8 INIT, NSTEP, NS, IPRINT, ISAVE, IRATIO, IEQUI
      INTEGER*8 MBMM, MCM, PREV(MNP)
      INTEGER*8 CYC(MNP), NSWAP

      REAL*8 DENS, TEMP, BETA, DENS LJ
      REAL*8 DRMAX, ALPHA, CDIM
      REAL*8 RANF, DURMY, SR9, SR3
      REAL*8 VLRC, VLRC6, VLRC12, WLRC, WLRC6, WLRC12
      REAL*8 ACM, ACATMA, ACATMAS, ACATMAB
      REAL*8 V, VNEW, VOLD, VEND, DELTV, VN, VS
      REAL*8 W, WNEW, WOLD, WEND, DELTW, WN, WS
      REAL*8 KE, KENEW, KEOLD, DELTKE, KEEND
      REAL*8 AVV, ACV, ACVSQ, FLV
      REAL*8 AVW, ACW, ACWSQ, FLW
      REAL*8 AVKE, ACKE, ACKESQ, FLKE
      REAL*8 ACT, ACTNEW, ACTOLD, DELTACT, DELTACTB
      REAL*8 RXIOLD(MDIM), RXINew(MDIM)
      REAL*8 RXP(MDIM,0:N), RXPP(MDIM,0:N)
      REAL*8 STD, PS, KKK, VVV, WWW
      REAL*8 RATIO, RATIOS, RATIOB
      REAL*8 WIND, ACWIND, SFI, SF, IC
      REAL*8 GA

      INTEGER*8 BIN, MAXBIN, MAXBIN2, HIST(1000000), ICALCG
      REAL*8 CONST, RLOWER, RUPPER
      REAL*8 TSTEP, NIDEAL, GR

      CHARACTER CNFILE*30, POTK*10
      LOGICAL OVRLAP, IFB, IFDISP, IFBRIDGE

C
C PI = ACOS(-1.d0)
C OPEN(UNIT = 16, FILE = 'back.dat', STATUS = 'UNKNOWN')
C OPEN(UNIT = 15, FILE = 'rdf.dat', STATUS = 'UNKNOWN')

C *****
C ** READ INPUT DATA **
C *****

      WRITE(*, '(***** PROGRAM PIMC *****)')
      WRITE(*, '(** PLANE WAVES **')
      WRITE(*, '(** PATH INTEGRAL MONTE CARLO PROGRAM **')
      OPEN(UNIT=10, FILE='data-gr-rs.in', STATUS='UNKNOWN')
      READ(10,*) I
      READ(10,*) DIM
      READ(10,*) I
      READ(10,*) SEED
      READ(10,*) I
      READ(10,*) IFB
      READ(10,*) I
      READ(10,*) NP
      READ(10,*) I
      READ(10,*(A')) POTK
      READ(10,*) I
      READ(10,*) FTNO
      READ(10,*) I
      READ(10,*) FTM
      READ(10,*) I
      READ(10,*) NSTEP
      READ(10,*) I
      READ(10,*) IPRINT
      READ(10,*) I
      READ(10,*) ISAVE
      READ(10,*) I
      READ(10,*) IEQUI
      READ(10,*) I
      READ(10,*) IRATIO
      READ(10,*) I
      READ(10,*) ICALCG
      READ(10,*) I
      READ(10,*(A')) CNFILE
      READ(10,*) I
      READ(10,*) INIT
      READ(10,*) I
      READ(10,*) RADIUS
      READ(10,*) I
      READ(10,*) TEMP
      READ(10,*) I
      READ(10,*) ALPHA
      READ(10,*) I
      READ(10,*) MBMM
      READ(10,*) I
      READ(10,*) RCUT
      READ(10,*) I
      READ(10,*) SIG
      READ(10,*) I
      READ(10,*) EPSR
      READ(10,*) I
      READ(10,*) EPSA
      READ(10,*) I
      READ(10,*) EPS
      READ(10,*) I
      READ(10,*) IFDISP
      READ(10,*) I
      READ(10,*) IFBRIDGE
      CLOSE(UNIT=10)
      WRITE(*, '(** IN DIMENSION (1,2,3,...)'I12/')) DIM
      WRITE(*, '(*****')
      GOTO 1111 ! comment if input from keyboard

      WRITE(*, '(***** PROGRAM PIMC *****)')
      WRITE(*, '(** PLANE WAVES **')
      WRITE(*, '(** PATH INTEGRAL MONTE CARLO PROGRAM **')

      WRITE(*, '(** ENTER THE SPATIAL DIMENSIONS **')
      READ(*,*) DIM
      WRITE(*, '(** ENTER SEED FOR RANDOM SEQUENCE **')
      READ(*,*) SEED
      WRITE(*, '(** IF BOSE (T/F) **')
      READ(*,*) IFB
      WRITE(*, '(** ENTER THE NUMBER OF PARTICLES < MNP **')
      READ(*,*) NP
      WRITE(*, '(** ENTER TYPE OF PAIR POTENTIAL (Many Body) **')
      READ(*,*(A')) POTK
      WRITE(*, '(** ENTER THE NUMBER OF DISCRETIZATIONS < N **')
      READ(*,*) FTNO
      WRITE(*, '(** ENTER THE BARE MASS **')
      READ(*,*) FTM
      WRITE(*, '(** ENTER NUMBER OF CYCLES **')
      READ(*,*) NSTEP
      WRITE(*, '(** ENTER NUMBER OF STEPS BETWEEN OUTPUT LINES **')
      READ(*,*) IPRINT
      WRITE(*, '(** ENTER NUMBER OF STEPS BETWEEN DATA SAVES **')
      READ(*,*) ISAVE
      WRITE(*, '(** ENTER NUMBER OF STEPS FOR EQUILIBRATION **')
      READ(*,*) IEQUI
      WRITE(*, '(** ENTER INTERVAL FOR UPDATE OF MAX. DISPL. **')
      READ(*,*) IRATIO
      WRITE(*, '(** ENTER INTERVAL FOR RDF CALCULATION **')
      READ(*,*) ICALCG
      WRITE(*, '(** ENTER THE CONFIGURATION FILE NAME **')
      READ(*,*(A')) CNFILE
      WRITE(*, '(** ENTER 0 INIT Z, 1 INIT, 2 REST C, 2 REST F **')
      READ(*,*) INIT
      WRITE(*, '(** ENTER THE SPHERE RADIUS **')
      READ(*,*) RADIUS
      WRITE(*, '(** ENTER THE TEMPERATURE **')
```

```

READ (*,*) TEMP
WRITE(*, '( " ENTER MAX. DISPLACEMENT DRMAX/SIGMA      " ) )
READ (*,*) ALPHA
WRITE(*, '( " ENTER MAXIMUM NUMBER OF BRIDGE TIMESLICES  " ) )
READ (*,*) MBMM
WRITE(*, '( " ENTER THE POTENTIAL CUTOFF DISTANCE ( " 2.5 " ) ) )
READ (*,*) RCUT
WRITE(*, '( " ENTER SIG      " ) )
READ (*,*) SIG
WRITE(*, '( " ENTER EPSR      " ) )
READ (*,*) EPSR
WRITE(*, '( " ENTER EPSA      " ) )
READ (*,*) EPSA
WRITE(*, '( " ENTER EPS      " ) )
READ (*,*) EPS
WRITE(*, '( " IF DISPLACEMENT MOVE (T/F)      " ) )
READ (*,*) IFDISP
WRITE(*, '( " IF BRIDGE MOVE (T/F)      " ) )
READ (*,*) IFBRIDGE
WRITE(*, '( " IN DIMENSION (1,2,3,...) " I2 / ) ) DIM
WRITE(*, '( " *****      " ) )

1111 CONTINUE

IF (MBMM.GT. FTNO) THEN
  WRITE(*,*) "number of timeslices in bridge > ",FTNO
  STOP
ENDIF

IF (DIM.NE. 2) THEN
  WRITE(*,*) "DIM not equal to 2"
  STOP
ENDIF

C ** INITIALIZE RANDOM NUMBER GENERATOR **

CALL SRAND ( SEED )
IF (SEED.EQ.1) THEN
  CALL SRAND ( 0 )
ENDIF

C ** DENSITY **

DENS = NP/4.0/PI/RADIUS**2

C ** INVERSE TEMPERATURE BETA **

BETA = (1.0/TEMP)

C ** IMAGINARY TIMESTEP **

LS = BETA/FTNO ! time step
STD = (LS/FTM)**0.5 ! standard deviation of free-particle

C ** MOMENT OF INERTIA OF A UNITARY SPHERICAL SHELL **

IC = 2*(NP*FTM)/3

C ** WRITE INPUT DATA **

WRITE(*, '( " SEED      " ,I10 ) ) SEED
WRITE(*, '( " POTENTIAL      " ,A ) ) POTK
WRITE(*, '( " DIMENSIONS      " ,I10 ) ) DIM
WRITE(*, '( " NUMBER OF PARTICLES      " ,I10 ) ) NP
WRITE(*, '( " NUMBER OF CYCLES      " ,I10 ) ) NSTEP
WRITE(*, '( " NUMBER OF EQUIL. STEPS      " ,I10 ) ) IEQUI
WRITE(*, '( " OUTPUT FREQUENCY      " ,I10 ) ) IPRINT
WRITE(*, '( " SAVE FREQUENCY      " ,I10 ) ) ISAVE
WRITE(*, '( " RATIO UPDATE FREQUENCY      " ,I10 ) ) IRATIO
WRITE(*, '( " CONFIGURATION FILE NAME      " ,A ) ) CNFILE
WRITE(*, '( " TEMPERATURE      " ,E10.4 ) ) TEMP
WRITE(*, '( " DENSITY      " ,E10.4 ) ) DENS
WRITE(*, '( " PARTICLE MASS      " ,E10.4 ) ) FTM
WRITE(*, '( " # TIME SLICES      " ,I10 ) ) FTNO
WRITE(*, '( " TIME STEP      " ,E10.4 ) ) LS

C ** CONVERT INPUT DATA TO PROGRAM UNITS **

C SIGMA = ( DBLE ( NP ) / DENS ) ** ( 1.0 / DIM )
SIGMA = 2*PI
SIGM(1) = PI
SIGM(2) = 2*PI
DRMAX = ALPHA * SIGMA

IF (POTK.EQ. 'LJ') THEN
  DENSLJ = DENS * SIG ** DBLE( DIM )
  RCUT = SIGMA/2.40/SIG
ENDIF

C MAXBIN = INT ( 2*RADIUS/DELR ) ! Euclidean
MAXBIN = INT ( PI*RADIUS/DELR ) ! Geodesic
MAXBIN2 = INT ( MAXBIN/2.0 )
DO I = 1, MAXBIN
  HIST(I) = 0
ENDDO

IF (DIM .eq. 3) CONST = 4.0 * PI * DENS / 3.0
IF (DIM .eq. 2) CONST = PI * DENS
IF (DIM .eq. 1) CONST = 2.0 * DENS

C ** INITIALIZE CONFIGURATION **

DO I = 1, NP
  NEXT(I) = I
  LEXT(I) = I
  DO J = 1, FTNO
    MEXT(J,I) = I
  ENDDO
ENDDO

C ** ZERO ACCUMULATORS **

ACV = 0.0
ACVSQ = 0.0
FLV = 0.0
ACW = 0.0
ACWSQ = 0.0
FLW = 0.0
ACKE = 0.0
ACKESQ = 0.0
FLKE = 0.0
ACWIND = 0.0
ACM = 0.0
ACATMA = 0.0
ACATMA2 = 0.0
ACATMAS = 0.0

IF ( INIT .EQ. 0 ) THEN
  PRINT*, "PATHS INITIALIZATION ....."
  RX=0. ! all paths zeroed
  NS = NSTEP
  OPEN (UNIT = 9, STATUS = 'UNKNOWN')
ELSEIF ( INIT .EQ. 1 ) THEN
  PRINT*, "PATHS INITIALIZATION ....."
C ** READ INITIAL CONFIGURATION **
  CALL INITONSPH ( CNFILE ) ! random configuration on equator
  CALL READCN ( CNFILE )
  NS = NSTEP
  OPEN (UNIT = 9, STATUS = 'UNKNOWN')
ELSEIF ( INIT .EQ. 2 ) THEN
  PRINT*, "RESTART FROM CONFIG ....."
C ** READ INITIAL CONFIGURATION **
  CALL READCN ( CNFILE )
  NS = NSTEP
  OPEN (UNIT = 9, STATUS = 'OLD', ACCESS = 'APPEND')
ELSEIF ( INIT .EQ. 3 ) THEN
  PRINT*, "RESTART FULL ....."
  CALL READCN ( CNFILE )
  READ(16,*) (HIST(I), I=1, MAXBIN),
  & ACV, ACVSQ, ACW, ACWSQ, ACKE, ACKESQ, ACWIND, ACM, NS
  NS=NS+NSTEP
  OPEN (UNIT = 9, STATUS = 'OLD', ACCESS = 'APPEND')
ELSE
  WRITE (*,*) 'INIT different from 0,1,2,3'
  STOP
ENDIF

C ** CALCULATE LONG RANGE CORRECTIONS **
C ** SPECIFIC TO THE LENNARD JONES FLUID **

IF (DIM .EQ. 1) CDIM = 1
IF (DIM .EQ. 2) CDIM = PI
IF (DIM .EQ. 3) CDIM = 2*PI

SR3 = - RCUT ** ( - 6. + DIM ) / ( - 6. + DIM )
SR9 = - RCUT ** ( - 12. + DIM ) / ( - 12. + DIM )

VLRC12 = 4 * EPS * CDIM * DENSLJ * NP * SR9
VLRC6 = - 4 * EPS * CDIM * DENSLJ * NP * SR3
VLRC = VLRC12 + VLRC6
WLRC12 = 4.0 * VLRC12
WLRC6 = 2.0 * VLRC6
WLRC = WLRC12 + WLRC6

C ** WRITE OUT SOME USEFUL INFORMATION **

WRITE(*, '( " SIGMA      " ,E10.4 ) ) SIGMA
WRITE(*, '( " MAXIMUM DISPLACEMENT      " ,E10.4 ) ) DRMAX

C ** CALCULATE INITIAL ENERGY AND CHECK FOR OVERLAPS **

CALL SUMUP ( POTK, OVRLAP, KE, V, W )

IF (POTK.EQ. 'LJ') THEN
  VS = ( V + VLRC )
  WS = ( W + WLRC )
ELSE
  VS = V
  WS = W
ENDIF

WRITE(*, '( " INITIAL V      " ,E10.4 ) ) VS
WRITE(*, '( " INITIAL W      " ,E10.4 ) ) WS
WRITE(*, '( " INITIAL KE      " ,E10.4 ) ) KE

WRITE(*, '( / / / START OF MARKOV CHAIN      " ) )
WRITE(*, '( " NMOVE      " ,I10 ) ) NMOVE
WRITE(*, '( " RATIO      " ,E10.4 ) ) RATIO
WRITE(*, '( " ACTION      " ,E10.4 ) ) ACTION

C *****
C ** LOOPS OVER ALL CYCLES AND ALL TIME SLICES **
C *****

DO 100 STEP = NS-NSTEP+1, NS

  CP = INT(FTNO*РАНF(DUMMY))+1 ! select a random timeslice
  MBM = INT((MBMM-1)*РАНF(DUMMY))+2 ! # timeslices in bridge
  IP = INT(NP*РАНF(DUMMY))+1 ! select a particle
  KP = INT(NP*РАНF(DUMMY))+1 ! select another particle
  IF (.NOT.IFB) KP = IP ! for boltzmann statistics
  IF (IFDISP) GOTO 77 ! uncommment if only displacement move

C *****
C ** BRIDGE&SWAP MOVE (ROSE STATISTICS) **
C *****

C direct mapping from sphere rx to plane rp
  call mappingd()
  call equiv(rpn,rp)

  mcm = cp+mbm-floor((cp+mbm-.1)/ftn0)*ftn0

  nip=next(ip)
  nkp=next(kp)

```

```

      vold=0.d0
      wold=0.d0
      if(cp+mbm.le.ftn0)then
        do i=cp+1,mcm-1
          call pppnrgy ( potk, rx(:,i,ip), ip,
            :           rx(:,i,kp), kp, i,
            :           vvv, www )
          vold=vold+vvv
          wold=wold+www
        enddo
      else
        do i=cp+1,ftn0
          call pppnrgy ( potk, rx(:,i,ip), ip,
            :           rx(:,i,kp), kp, i,
            :           vvv, www )
          vold=vold+vvv
          wold=wold+www
        enddo
        do i=1,mcm-1
          call pppnrgy ( potk, rx(:,i,nip), nip,
            :           rx(:,i,nkp), nkp, i,
            :           vvv, www )
          vold=vold+vvv
          wold=wold+www
        enddo
      endif
      keold=0.d0
      do k=1,np
        if(k.eq.ip.or.k.eq.kp.or.k.eq.nip.or.k.eq.nkp)then
          do i=1,ftn0
            call kknergy ( rx(:,i,k), k, i,
              :           kkk )
            keold=keold+kkk
          enddo
        endif
      enddo
      deltke=keold-keold

c    calculate the ratio of transition probabilities
      call gauss(cp,ga)

c    inverse mapping
      call equiv(rp,rpn)
      call equiv(rpn,rx)
      call mappingi()

      keneu=0.d0
      do k=1,np
        if(k.eq.ip.or.k.eq.kp.or.k.eq.nip.or.k.eq.nkp)then
          do i=1,ftn0
            call kknergy ( rx(:,i,k), k, i,
              :           kkk )
            keneu=keneu+kkk
          enddo
        endif
      enddo
      deltke=keneu-keold

c    calculate the acceptance probability
      call acc_p(deltv,deltke,ps)
      ps=ps*ga

c    accept/reject
      if (ps.gt.ranf(dummy)) then
        ke=ke+deltke
        v=v+vnew-vold
        w=w+wnew-wold
      else
        call equiv(rx,rpn)
        acatmab = acatmab - 1.d0
        if (ip.ne.kp) then
          call switch(next(ip),next(kp))
          call switch(next(cp,ip),next(cp,kp))
          acatmas = acatmas - 1.d0
        endif
      endif

c    build the permutations cycles in text
      call permcy()
c    count number of swaps of two particles
      call cycles(cyc,nswap)

c    balance ke between bridge and displace
c    call sumupke ( ke )

      IF (STEP.GT.IEQUI) THEN
        ACM = ACM + 1.0

C    ** CALCULATE INSTANTANEOUS VALUES **

      IF (POTK .EQ. 'LJ') THEN
        VN = ( V + VLRC )
      ELSE
        VN = V - W
        WN = W
      ENDIF
      CALL C'WIND( WIND )
      IF (WIND.GT.3*BETA*IC*2/FTM**2) WIND=3*BETA*IC*2/FTM**2

C    ** ACCUMULATE AVERAGES **

      ACV   = ACV   + VN
      ACVSQ = ACVSQ + VN*VN
      ACW   = ACW   + WN
      ACWSQ = ACWSQ + WN*WN
      ACKE  = ACKE  + KE
      ACKESQ = ACKESQ + KE*KE
      ACWIND = ACWIND + WIND
    ENDIF

      IF (IFBRIDGE) GOTO 97

C    *****
C    ** ENDS BRIDGE&SWAP MOVE **
C    *****

77    CONTINUE

C    *****
C    ** DISPLACEMENT MOVE **
C    *****

C    ** PREVIOUS IP **

      DO I=1,NP
        J=NEXT(I)
        PREV(J)=I
      ENDDO

      NIP = NEXT(IP)
      PIP = PREV(IP)

      DO 90 C1 = 1, FTNO

        DO IDIM = 1, DIM
          RXIOLD(IDIM) = RX(IDIM,C1,IP)
        ENDDO

C    ** CALCULATE THE ENERGY OF I IN THE OLD CONFIGURATION **

      CALL PENRGY ( POTK, RXIOLD, IP, C1,
        :           VOLD, WOLD )

```

```

      CALL KENERGY ( RXIOLD, IP, C1,
:      KEOLD )
C  ** INSTANTANEOUS VALUE OF THE ACTION **
      ACTOLD = KEOLD + VOLD
C  ** MOVE I AND PICKUP THE CENTRAL IMAGE **
      DO IDIM = 1, DIM
        RXINEW(IDIM) = RXIOLD(IDIM) +
:      ( 2.0 * RANF ( DUMMY ) - 1.0 ) * DRMAX
        RXINEW(IDIM) = RXINEW(IDIM) -
:      DWINT ( RXINEW(IDIM)/SIGM(IDIM) ) * SIGM(IDIM)
      ENDDO
C  ** CALCULATE THE ENERGY OF I IN THE NEW CONFIGURATION **
      CALL PENERGY ( POTK, RXINEW, IP, C1,
:      VNEW, WNEW )
      CALL KENERGY ( RXINEW, IP, C1,
:      KENEW )
C  ** INSTANTANEOUS VALUE OF THE ACTION **
      ACTNEW = KENEW + VNEW
      DELTV = VNEW - VOLD
      DELTW = WNEW - WOLD
      DELTKE = KENEW - KEOLD
C  ** CHECK FOR ACCEPTANCE **
      DELTACT = ACTNEW - ACTOLD
      DELTACTB = LS*DELTACT
      IF ( EXP ( - DELTACTB ) .GT. RANF ( DUMMY ) ) THEN
        V = V + DELTV
        W = W + DELTW
        KE = KE + DELTKE
        ACATMA = ACATMA + 1.0
        DO IDIM = 1, DIM
          RX(IDIM,C1,IP) = RXINEW(IDIM)
C  IMAGINARY TIME PERIODIC BOUNDARY CONDITIONS
          IF (C1.EQ.1) THEN
            RX(IDIM,FTNO+1,PIP)=RX(IDIM,C1,IP)
          ENDIF
          IF (C1.EQ.FTNO) THEN
            RX(IDIM,0,NIP)=RX(IDIM,C1,IP)
          ENDIF
        ENDDO
      ENDIF
      IF (STEP.GT.IEQUI) THEN
        ACM = ACM + 1.0
C  ** CALCULATE INSTANTANEOUS VALUES **
C  HISTOGRAM FOR g(r)
      IF ( MOD ( C1, ICALCG ) .EQ. 0 ) THEN
        CALL GOFRC ( C1, MAXBIN, HIST )
      ENDIF
      IF (POTK .EQ. 'LJ') THEN
        VN = ( V + VLRC )
      ELSE
        VN = V - W
        WN = W
      ENDIF
      CALL CWIND( WIND )
      IF (WIND.GT.3*BETA*IC/2/FTM**2) WIND=3*BETA*IC/2/FTM**2
C  ** ACCUMULATE AVERAGES **
      ACV = ACV + VN
      ACVSQ = ACVSQ + VN*VN
      ACW = ACW + WN
      ACWSQ = ACWSQ + WN*WN
      ACKE = ACKE + KE
      ACKESQ = ACKESQ + KE*KE
      ACWIND = ACWIND + WIND
      ENDIF
C  *****
C  ** END DISPLACEMENT MOVE **
C  *****
90    CONTINUE
C  *****
C  ** ENDS LOOP OVER TIME SLICES **
C  *****
97    CONTINUE
C  ** WRITE OUT THE INSTANTANEOUS VALUES ON FORT.9 **
      SFI = WIND *FTM**2/BETA/IC/2
      SF = ACWIND*FTM**2/BETA/IC/2/ACM
      CALL FLUSH(9)
      IF ( MOD ( STEP, IPRINT ) .EQ. 0 ) THEN
        WRITE(9,*) STEP, DIM*NP/2/LS-KE/FTNO, VN/FTNO, WN/FTNO, SFI
      ENDIF
C  ** CREATE POSITION DISTRIBUTION **
C  CALL DISTR(30_8,STEP*FTNO*NP/30)
C  ** PERFORM PERIODIC OPERATIONS **
      IF ( MOD ( STEP, IRATIO ) .EQ. 0 ) THEN
C  ** ADJUST MAXIMUM DISPLACEMENT **
        RATIO = ACATMA / DBLE ( FTNO * IRATIO )
        RATIOB = ACATMAB / DBLE ( IRATIO )
        RATIOS = ACATMAS / DBLE ( IRATIO )
        IF ( RATIO .GT. 0.5 ) THEN
C  DRMAX = DRMAX * 1.05
        ELSE
C  DRMAX = DRMAX * 0.95
        ENDIF
        ACATMA = 0.0
        ACATMAB = 0.0
        ACATMAS = 0.0
      ENDIF
      IF ( MOD ( STEP, IPRINT ) .EQ. 0 ) THEN
C  ** WRITE OUT RUNTIME INFORMATION **
        WRITE(*,*) '      step      acm dr/sig ard
:      arb      ars'
        WRITE(*, '(2(2XI13),(2Xf6.4),4(2Xf8.6))') STEP, INT(ACM),
:      ALPHA, RATIO, RATIOB, RATIOS
        WRITE(*,*) '      ke      v      w
:      sf'
        WRITE(*, '(4(2XE13.7))') KE/FTNO, VN/FTNO, WN/FTNO,
:      SFI
        WRITE(*,*) '      <ke>      <v>      <w>
:      <sf>'
        WRITE(*, '(4(2XE13.7))') ACKE/ACM/FTNO, ACV/ACM/FTNO,
:      ACW/ACM/FTNO, SF
        WRITE(*,*) '      nswap'
        WRITE(*, '(I3)') NSWAP
      ENDIF
      IF ( MOD ( STEP, ISAVE ) .EQ. 0 ) THEN
C  ** WRITE OUT THE CONFIGURATION AT INTERVALS **
        CALL WRITCN ( CNFILE )
        REWIND(16)
        CALL FLUSH(16)
        WRITE(16,*) (HIST(I), I=1, MAXBIN),
&      ACV, ACVSQ, ACW, ACWSQ, ACKE, ACKESQ, ACWIND, ACM, STEP
C  ** WRITE OUT THE g(r) **
        IF ( STEP .GT. IEQUI ) THEN
          TSTEP = DBLE((STEP - IEQUI)*INT(FTNO/ICALCG))
          REWIND(15)
          DO BIN = 1, MAXBIN
            RLOWER = DBLE ( BIN - .5 ) * DELR
            RUPPER = RLOWER + DELR
            NIDEAL = (RUPPER/2/RADIUS)**DIM-
:      (RLOWER/2/RADIUS)**DIM
            GR = DBLE(HIST(BIN))/TSTEP/DBLE(NP)**2/NIDEAL
            CALL FLUSH(15)
            WRITE (15,*) DBLE(BIN-1)*DELR, GR
          ENDDO
        ENDIF
      ENDIF
100  CONTINUE
C  *****
C  ** ENDS THE LOOP OVER CYCLES **
C  *****
      WRITE(*, '(/' END OF MARKOV CHAIN '(/)')
C  ** CHECKS FINAL VALUE OF THE POTENTIAL ENERGY IS CONSISTENT **
      CALL SUMUP (POTK, OVRLAP, KEEND, VEND, WEND)
      IF ( ABS(VEND - V) .GT. 1.0d-03 ) THEN
        WRITE(*, '( ' PROBLEM WITH V ENERGY !!! ' ) )
        WRITE(*, '( ' VEND = ', E20.6 ' ) ) VEND
        WRITE(*, '( ' V = ', E20.6 ' ) ) V
      ENDIF
      IF ( ABS(KEEND - KE) .GT. 1.0d-03 ) THEN
        WRITE(*, '( ' PROBLEM WITH KE ENERGY !!! ' ) )
        WRITE(*, '( ' KEEND = ', E20.6 ' ) ) KEEND
        WRITE(*, '( ' KE = ', E20.6 ' ) ) KE
      ENDIF
C  ** WRITE OUT THE FINAL CONFIGURATION FROM THE RUN **
      CALL WRITCN ( CNFILE )
C  ** CALCULATE AND WRITE OUT RUNNING AVERAGES **
      AVV = ACV / ACM
      ACVSQ = ( ACVSQ / ACM ) - AVV ** 2

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      AVKE  = ACKE / ACM
      ACKESQ = ( ACKESQ / ACM ) - AVKE ** 2

C  ** CALCULATE FLUCTUATIONS **

      IF ( ACVSQ .GT. 0.0 ) FLV = SQRT ( ACVSQ/ACM )/FTN0
      IF ( ACKESQ .GT. 0.0 ) FLKE = SQRT ( ACKESQ/ACM )/FTN0

      WRITE(*, '(// AVERAGES '// )')
      WRITE(*, '(// <V/N>          = ',E12.6)') AVV/FTN0
      WRITE(*, '(// <KE/N>         = ',E12.6)') AVKE/FTN0

      WRITE(*, '(// FLUCTUATIONS '// )')

      WRITE(*, '(// FLUCTUATION IN <V/N> = ',E12.6)') FLV
      WRITE(*, '(// FLUCTUATION IN <KE/N> = ',E12.6)') FLKE
      WRITE(*, '(// END OF SIMULATION '// )')

C  *****
C  *****
C  *****
C  ** THE END
C  *****
C  *****
C  *****
      CLOSE(UNIT = 9 )
      CLOSE(UNIT = 15)
      CLOSE(UNIT = 16)
      STOP
      END

      subroutine permcyc()
      implicit none
! given a particle i, lext(i) returns the cycle it belongs to
      INCLUDE 'mc-sph.par'

      integer*8 i,j,k,ii(mmp),jj,kk,ll

      kk=1
      do i=1,np
        ll=1
        ii(ll)=i
        jj=next(ii(ll))
1       do j=1,ll
          if(jj.eq.ii(j))goto 2
        enddo
        ll=ll+1
        ii(ll)=jj
        goto 1
2       do k=1,ll
          lext(ii(k))=kk
        enddo
        kk=kk+1
      enddo

      return
      end

      subroutine cycles(cyc,ns)
      implicit none
! cyc(i) returns the number of particles in cycle of type i
! ns returns the total number of 2 particles swaps
      INCLUDE 'mc-sph.par'
      integer*8 i,cyc(mnp),ns

      ns=0
      cyc=0
      do i=1,np
        cyc(lext(i))=cyc(lext(i))+1
      enddo
      do i=1,np
        if (cyc(i).ne.0) ns=ns+cyc(i)-1
      enddo

      return
      end

      subroutine switch(i,j)
! switch i and j
      implicit none
      integer*8 i,j,k
      k=i
      i=j
      j=k
      return
      end

      subroutine acc_p(dv,dke,p)
      implicit none
! complete acceptance probability
      INCLUDE 'mc-sph.par'

      real*8 p,dke,dv

      p=exp(-ls*dv)      ! contribution from the pair potential
      p=p*exp(-ls*dke)    ! contribution from the kinetic energy

      return
      end

      subroutine updaten(j,rxp,ip,nip)
      implicit none
! updates a portion of the current path x using the proposed path xp
      INCLUDE 'mc-sph.par'

      integer*8 ip,nip,kp,nkp,j,l,k,ldim

```

```

      integer*8 mcm
      real*8 rxp(mdim,0:n)

      mcm = j+mbm-floor((j+mbm-.1)/ftn0)*ftn0

      l=0
      if(j+mbm.le.ftn0)then
        do k=j+1,mcm-1
          l=l+1
          do idim=1,ldim
            rpn(idim,k,ip)=rxp(idim,l)
          enddo
        enddo
      else
        do k=j+1,ftn0
          l=l+1
          do idim=1,ldim
            rpn(idim,k,ip)=rxp(idim,l)
          enddo
        enddo
        do k=1,mcm-1
          l=l+1
          do idim=1,ldim
            rpn(idim,k,nip)=rxp(idim,l)
          enddo
        enddo
        do idim=1,ldim
          rpn(idim,ftn0+1,ip)=rpn(idim,1,nip)
          rpn(idim,0,nip)=rpn(idim,ftn0,ip)
        enddo

      return
      end

      subroutine swapn(j,ip,nip,kp,nkp)
      implicit none
! swap the final part of the paths
      INCLUDE 'mc-sph.par'

      integer*8 ip,nip,kp,nkp,j,k,ldim
      integer*8 mcm
      real*8 rr

      mcm = j+mbm-floor((j+mbm-.1)/ftn0)*ftn0

      if(j+mbm.le.ftn0)then
        do k=mcm,ftn0
          do idim=1,ldim
            rr=rpn(idim,k,ip)
            rpn(idim,k,ip)=rpn(idim,k,kp)
            rpn(idim,k,kp)=rr
          enddo
        enddo
        do idim=1,ldim
          rpn(idim,ftn0+1,ip)=rpn(idim,1,nkp)
          rpn(idim,ftn0+1,kp)=rpn(idim,1,nip)
          rpn(idim,0,nip)=rpn(idim,ftn0,kp)
          rpn(idim,0,nkp)=rpn(idim,ftn0,ip)
        enddo
      endif
      return
      end

      subroutine bridge(x0,x1,std,xnew,out)
      implicit none
! sample m gaussians with std from xnew(0)=x0 to xnew(ftn0)=x1
      INCLUDE 'mc-sph.par'

      integer*8 l1,l2,l3,j,ldim,out
      real*8 std,d,s,x1
      real*8 x0(mdim),x1(mdim),xnew(mdim,0:n)

      l3=mbm
      do idim=1,ldim
        xnew(idim,0)=x0(idim)
        xnew(idim,l3)=x0(idim)+(x1(idim)-x0(idim))-
          dnint((x1(idim)-x0(idim))/sigm(idim))*sigm(idim)
      enddo
      do j=1,mbm-1
        l1=j-1
        l2=j
        s=std*(dble(l3-l2)/dble(l3-l1))*0.5d0
        do idim=1,ldim
          d=xnew(idim,l3)-xnew(idim,l1)
          d=d-dnint(d/sigm(idim))*sigm(idim)
          xnew(idim,j)=xnew(idim,l1)+d/dble(l3-l1)+xi(s)
          xnew(idim,j)=xnew(idim,j)-
            dnint(xnew(idim,j)/sigm(idim))*sigm(idim)
        enddo
      enddo
      return
      end

      function xi(std)
! sample a gaussian with standard deviation std (box-muller method)
      implicit none
      real*8 xi,std,pi,ranf
      data pi/3.14159265358979323846264338328d0/
      xi=cos(pi*ranf(0.d0))*std*sqrt(-2.d0*log(tiny(pi)+ranf(0.d0)))
      return
      end

      SUBROUTINE DISTR(NN,NORM)
      IMPLICIT NONE
C  WRITES ON FORT.10 THE X-POSITION DISTRIBUTION
      INCLUDE 'mc-sph.par'

```

```

REAL*8      DS,DIST(0:1000)
INTEGER*8    NN,NORM,I,J,K
SAVE        DIST

DS=SIGMA/NN

DO I=0,NN
  DO J=1,FTNO
    DO K=1,NP
      IF(-SIGMA/2+(I-.5)*DS.LT.RX(1,J,K).AND.
:      RX(1,J,K).LT.-SIGMA/2+(I+.5)*DS) THEN
        DIST(I)=DIST(I)+1.DO
      ENDIF
    ENDDO
  ENDDO
  WRITE(10,*) -SIGMA/2+I*DS,DIST(I)/NORM
ENDDO

CLOSE(UNIT=10)

RETURN
END

FUNCTION FACT ( N )
  IMPLICIT NONE
C  FACTORIAL FUNCTION
  INTEGER*8 FACT,N,P,I
  P=1
  DO I=1,N
    P=P*I
  ENDDO
  FACT=P
END

SUBROUTINE SUMUP (POTK, OVRLAP, KE, V, W)
  IMPLICIT NONE
C  *****
C  ** CALCULATES THE TOTAL ENERGY **
C  ** **
C  ** USAGE: **
C  ** **
C  ** THE SUBROUTINE RETURNS THE TOTAL ENERGY AT THE **
C  ** BEGINNING AND END OF THE RUN. **
C  *****
  INCLUDE 'mc-sph.par'

  REAL*8      V, KE, VV, KK
  LOGICAL     OVRLAP
  CHARACTER   POTK*(*)

  REAL*8      RXII, RXIJ, RYIJ, RZIJ
  REAL*8      VIJ, WIJ, RIJSQ, W, WW

  INTEGER*8    TAU, I, J, IDIM

C  POTENTIAL ACTION

  VV = 0.0
  WW = 0.0

C  ** LOOP OVER ALL THE PAIRS IN THE LIQUID **

  DO TAU = 1, FTNO
    DO 100 I = 1, NP - 1
      DO 99 J = I + 1, NP
        RIJSQ = 0.d0
        DO IDIM = 1, DIM
          RXIJ = RX(IDIM,TAU,I) - RX(IDIM,TAU,J)
C  ** MINIMUM IMAGE THE PAIR SEPARATIONS **
          RXIJ = RXIJ -
:          DNINT ( RXIJ/SIGM(IDIM) ) * SIGM(IDIM)
          RIJSQ = RIJSQ + RXIJ * RXIJ
        ENDDO
C  ** EUCLIDEAN DISTANCE
        RXIJ = COS(RX(1,TAU,I))*COS(RX(1,TAU,J))*
:        COS(RX(2,TAU,I))*COS(RX(2,TAU,J))
        RYIJ = COS(RX(1,TAU,I))*COS(RX(1,TAU,J))*
:        SIN(RX(2,TAU,I))*SIN(RX(2,TAU,J))
        RZIJ = SIN(RX(1,TAU,I))*SIN(RX(1,TAU,J))
        RIJSQ = RXIJ + RYIJ + RZIJ
        RIJSQ = RADIUS**2*(2*(1.-RIJSQ))

        CALL POT (RIJSQ, VIJ, WIJ, POTK)
C  VV = VV + VIJ
C  WW = WW + WIJ
99      CONTINUE
        VV = VV - LOG(ABS(RADIUS**2*COS(RX(1,TAU,I))))/LS
        WW = WW - LOG(ABS(RADIUS**2*COS(RX(1,TAU,I))))/LS
100     CONTINUE
        VV = VV - LOG(ABS(RADIUS**2*COS(RX(1,TAU,NP))))/LS
        WW = WW - LOG(ABS(RADIUS**2*COS(RX(1,TAU,NP))))/LS
      ENDDO
    ENDDO
    V = VV
    W = WW

C  KINETIC ACTION

    KK = 0.0

    DO TAU = 1, FTNO
      DO I = 1, NP
        RXII = RX(1,TAU,I)-RX(1,TAU+1,I)
        RXII = RXII - DNINT ( RXII/SIGM(1) ) * SIGM(1)
        KK=KK+FTM*(RADIUS*COS(RX(1,TAU,I))*RXII)**2./(2.DO*LS**2.)

        RXII = RX(2,TAU,I)-RX(2,TAU+1,I)
        RXII = RXII - DNINT ( RXII/SIGM(2) ) * SIGM(2)
        KK=KK+FTM*(RADIUS*COS(RX(1,TAU,I))*RXII)**2./(2.DO*LS**2.)

        RXII = RX(1,TAU,I)-RX(1,TAU+1,I)
        RXII = RXII - DNINT ( RXII/SIGM(1) ) * SIGM(1)
        KK=KK+FTM*(RADIUS*COS(RX(1,TAU,I))*RXII)**2./(2.DO*LS**2.)

        RXII = RX(2,TAU,I)-RX(2,TAU+1,I)
        RXII = RXII - DNINT ( RXII/SIGM(2) ) * SIGM(2)
        KK=KK+FTM*(RADIUS*COS(RX(1,TAU,I))*RXII)**2./(2.DO*LS**2.)

      ENDDO
    ENDDO
    KE = KK

    RETURN
  END

SUBROUTINE SUMUPKE ( KE )
  IMPLICIT NONE
C  *****
C  ** CALCULATES THE TOTAL ENERGY **
C  ** **
C  ** USAGE: **
C  ** **
C  ** THE SUBROUTINE RETURNS THE TOTAL ENERGY AT THE **
C  ** BEGINNING AND END OF THE RUN. **
C  *****
  INCLUDE 'mc-sph.par'

  REAL*8      KE, KK, RXII
  INTEGER*8    TAU, I

C  KINETIC ACTION

  KK = 0.0

  DO TAU = 1, FTNO
    DO I = 1, NP
      RXII = RX(1,TAU,I)-RX(1,TAU+1,I)
      RXII = RXII - DNINT ( RXII/SIGM(1) ) * SIGM(1)
      KK=KK+FTM*(RADIUS*COS(RX(1,TAU,I))*RXII)**2./(2.DO*LS**2.)

      RXII = RX(2,TAU,I)-RX(2,TAU+1,I)
      RXII = RXII - DNINT ( RXII/SIGM(2) ) * SIGM(2)
      KK=KK+FTM*(RADIUS*COS(RX(1,TAU,I))*RXII)**2./(2.DO*LS**2.)

    ENDDO
  ENDDO
  KE = KK

  RETURN
END

SUBROUTINE PENERGY ( POTK, RXI, I, TAU,
:  V, W )
  IMPLICIT NONE
C  *****
C  ** RETURNS THE POTENTIAL ENERGY OF ATOM I WITH ALL OTHER ATOMS. **
C  ** **
C  ** PRINCIPAL VARIABLES: **
C  ** **
C  ** INTEGER I          THE ATOM OF INTEREST **
C  ** INTEGER NP         THE NUMBER OF ATOMS **
C  ** INTEGER TAU        THE TIMESTEP **
C  ** REAL*8 RX, RY, RZ  THE ATOM POSITIONS **
C  ** REAL*8 RXI,RYI,RZI THE COORDINATES OF ATOM I **
C  ** REAL*8 V           THE POTENTIAL ENERGY OF ATOM I **
C  ** REAL*8 W           THE VIRIAL OF ATOM I **
C  ** **
C  ** USAGE: **
C  ** **
C  ** THIS SUBROUTINE IS USED TO CALCULATE THE CHANGE OF ENERGY **
C  ** DURING A TRIAL MOVE OF ATOM I. IT IS CALLED BEFORE AND **
C  ** AFTER THE RANDOM DISPLACEMENT OF I. **
C  *****
  INCLUDE 'mc-sph.par'

  REAL*8      RXI(MDIM), V, W
  INTEGER*8    I, J, TAU, IDIM
  CHARACTER   POTK*(*)

  REAL*8      RXIJ, RYIJ, RZIJ, RIJSQ, VIJ, WIJ

  V = 0.0
  W = 0.0

C  ** LOOP OVER ALL MOLECULES EXCEPT I **

  DO J = 1, NP
    IF ( I .NE. J ) THEN
      RIJSQ = 0.d0
      DO IDIM = 1, DIM
        RXIJ = RXI(IDIM) - RX(IDIM,TAU,J)
C  RXIJ = RXIJ -
C  DNINT ( RXIJ/SIGM(IDIM) ) * SIGM(IDIM)
      RIJSQ = RIJSQ + RXIJ * RXIJ
      ENDDO

      RXIJ = RXIJ -
:      DNINT ( RXIJ/SIGM(IDIM) ) * SIGM(IDIM)
      RIJSQ = RIJSQ + RXIJ * RXIJ
      ENDDO

      RXIJ = COS(RXI(1))*COS(RX(1,TAU,J))*
:      COS(RXI(2))*COS(RX(2,TAU,J))
      RYIJ = COS(RXI(1))*COS(RX(1,TAU,J))*
:      SIN(RXI(2))*SIN(RX(2,TAU,J))
      RZIJ = SIN(RXI(1))*SIN(RX(1,TAU,J))
      RIJSQ = RXIJ + RYIJ + RZIJ
      RIJSQ = RADIUS**2*(2*(1.-RIJSQ))

      CALL POT (RIJSQ, VIJ, WIJ, POTK)
      V = V + VIJ
      W = W + WIJ
    ENDIF
  ENDDO

  V = V - LOG(ABS(RADIUS**2*COS(RXI(1))))/LS
  W = W - LOG(ABS(RADIUS**2*COS(RXI(1))))/LS

  RETURN

```

```

END

SUBROUTINE PPPENERGY ( POTK, RXI, I, RXJ, J,
:   TAU, V, W )
  IMPLICIT NONE
  *****
  C ** RETURNS THE POTENTIAL ENERGY OF ATOMS I AND J WITH **
  C ** ALL OTHER ATOMS PLUS THE ONE BETWEEN I AND J **
  C **
  C ** PRINCIPAL VARIABLES: **
  C **
  C ** INTEGER I, J          THE ATOMS OF INTEREST **
  C ** INTEGER NP           THE NUMBER OF ATOMS **
  C ** INTEGER TAU          THE TIMESTEP **
  C ** REAL*8 RX, RY, RZ    THE ATOM POSITIONS **
  C ** REAL*8 RXI,RYI,RZI   THE COORDINATES OF ATOM I **
  C ** REAL*8 RXJ,RYJ,RZJ   THE COORDINATES OF ATOM J **
  C ** REAL*8 V             THE POTENTIAL ENERGY OF ATOM I **
  C ** REAL*8 W             THE VIRIAL OF ATOM I **
  C **
  C ** USAGE: **
  C **
  C ** THIS SUBROUTINE IS USED TO CALCULATE THE CHANGE OF ENERGY **
  C ** DURING A TRIAL MOVE OF ATOM I. IT IS CALLED BEFORE AND **
  C ** AFTER THE RANDOM DISPLACEMENT OF I. **
  C *****
  INCLUDE 'mc-sph.par'

  REAL*8 RXI(MDIM), RXJ(MDIM), V, W
  INTEGER*8 I, J, K, TAU, IDIM
  CHARACTER POTK(*)

  REAL*8 RXIJ, RYIJ, RZIJ, RIJSQ, VIJ, WIJ

  V = 0.0
  W = 0.0

  C ** LOOP OVER ALL MOLECULES EXCEPT I AND J **

  DO 100 K = 1, NP
    IF ( K.NE. I .AND. K.NE. J ) THEN
      RIJSQ = 0.d0
      DO IDIM = 1, DIM
        RXIJ = RXI(IDIM) - RX(IDIM,TAU,K)
      C
      RXIJ = RXIJ -
      :   DNINT ( RXIJ/SIGM(IDIM) ) * SIGM(IDIM)
      C
      RIJSQ = RIJSQ + RXIJ * RXIJ
      C
      ENDDO

      C ** EUCLIDEAN DISTANCE
      RXIJ = COS(RXI(1))*COS(RX(1,TAU,K))*
      :   COS(RXI(2))*COS(RX(2,TAU,K))
      C
      RYIJ = COS(RXI(1))*COS(RX(1,TAU,K))*
      :   SIN(RXI(2))*SIN(RX(2,TAU,K))
      C
      RZIJ = SIN(RXI(1))*SIN(RX(1,TAU,K))
      RIJSQ = RXIJ + RYIJ + RZIJ
      RIJSQ = RADIUS**2*(2*(1.-RIJSQ))

      CALL POT (RIJSQ, VIJ, WIJ, POTK)
      V = V + VIJ
      W = W + WIJ

      IF ( I.NE. J ) THEN
        RIJSQ = 0.d0
        DO IDIM = 1, DIM
          RXIJ = RXJ(IDIM) - RX(IDIM,TAU,K)
        C
          RXIJ = RXIJ -
          :   DNINT ( RXIJ/SIGM(IDIM) ) * SIGM(IDIM)
          C
          RIJSQ = RIJSQ + RXIJ * RXIJ
          C
          ENDDO

        C ** EUCLIDEAN DISTANCE
        RXIJ = COS(RXJ(1))*COS(RX(1,TAU,K))*
        :   COS(RXJ(2))*COS(RX(2,TAU,K))
        C
        RYIJ = COS(RXJ(1))*COS(RX(1,TAU,K))*
        :   SIN(RXJ(2))*SIN(RX(2,TAU,K))
        C
        RZIJ = SIN(RXJ(1))*SIN(RX(1,TAU,K))
        RIJSQ = RXIJ + RYIJ + RZIJ
        RIJSQ = RADIUS**2*(2*(1.-RIJSQ))

        CALL POT (RIJSQ, VIJ, WIJ, POTK)
        V = V + VIJ
        W = W + WIJ
      C
      ENDDIF
    C
    ENDDIF
  100 CONTINUE

  C
  RETURN

  V = V - LOG(ABS(RADIUS**2*COS(RXI(1))))/LS
  W = W - LOG(ABS(RADIUS**2*COS(RXI(1))))/LS

  IF (I.NE. J) THEN
    DO IDIM = 1, DIM
      RXIJ = RXI(IDIM) - RXJ(IDIM)
    C
      RXIJ = RXIJ -
      :   DNINT ( RXIJ/SIGM(IDIM) ) * SIGM(IDIM)
      C
      RIJSQ = RIJSQ + RXIJ * RXIJ
      C
      ENDDO

    C ** EUCLIDEAN DISTANCE
    RXIJ = COS(RXI(1))*COS(RXJ(1))*
    :   COS(RXI(2))*COS(RXJ(2))
    C
  C
  *****
  SUBROUTINE PPENERGY ( POTK, RPI, I, RPJ, J,
:   TAU, V, W )
    IMPLICIT NONE
    *****
    C ** RETURNS THE POTENTIAL ENERGY OF ATOMS I AND J WITH **
    C ** ALL OTHER ATOMS PLUS THE ONE BETWEEN I AND J **
    C **
    C ** PRINCIPAL VARIABLES: **
    C **
    C ** INTEGER I, J          THE ATOMS OF INTEREST **
    C ** INTEGER NP           THE NUMBER OF ATOMS **
    C ** INTEGER TAU          THE TIMESTEP **
    C ** REAL*8 RX, RY, RZ    THE ATOM POSITIONS **
    C ** REAL*8 RXI,RYI,RZI   THE COORDINATES OF ATOM I **
    C ** REAL*8 RXJ,RYJ,RZJ   THE COORDINATES OF ATOM J **
    C ** REAL*8 V             THE POTENTIAL ENERGY OF ATOM I **
    C ** REAL*8 W             THE VIRIAL OF ATOM I **
    C **
    C ** USAGE: **
    C **
    C ** THIS SUBROUTINE IS USED TO CALCULATE THE CHANGE OF ENERGY **
    C ** DURING A TRIAL MOVE OF ATOM I. IT IS CALLED BEFORE AND **
    C ** AFTER THE RANDOM DISPLACEMENT OF I. **
    C *****
    INCLUDE 'mc-sph.par'

    REAL*8 RPI(MDIM), RPJ(MDIM), RXI(MDIM), RXJ(MDIM), V, W
    INTEGER*8 I, J, K, TAU, IDIM
    CHARACTER POTK(*)

    REAL*8 RXIJ, RYIJ, RZIJ, RIJSQ, VIJ, WIJ

    C
    C MAPPING
    RXI(1)=RPI(1)
    RXI(2)=RPJ(2)
    RXJ(1)=RPJ(1)
    RXJ(2)=RPJ(2)

    V = 0.0
    W = 0.0

    C ** LOOP OVER ALL MOLECULES EXCEPT I AND J **

    DO 100 K = 1, NP
      IF ( K.NE. I .AND. K.NE. J ) THEN
        RIJSQ = 0.d0
        DO IDIM = 1, DIM
          RXIJ = RXI(IDIM) - RX(IDIM,TAU,K)
        C
          RXIJ = RXIJ -
          :   DNINT ( RXIJ/SIGM(IDIM) ) * SIGM(IDIM)
          C
          RIJSQ = RIJSQ + RXIJ * RXIJ
          C
          ENDDO

        C ** EUCLIDEAN DISTANCE
        RXIJ = COS(RXI(1))*COS(RX(1,TAU,K))*
        :   COS(RXI(2))*COS(RX(2,TAU,K))
        C
        RYIJ = COS(RXI(1))*COS(RX(1,TAU,K))*
        :   SIN(RXI(2))*SIN(RX(2,TAU,K))
        C
        RZIJ = SIN(RXI(1))*SIN(RX(1,TAU,K))
        RIJSQ = RXIJ + RYIJ + RZIJ
        RIJSQ = RADIUS**2*(2*(1.-RIJSQ))

        CALL POT (RIJSQ, VIJ, WIJ, POTK)
        V = V + VIJ
        W = W + WIJ

        IF ( I.NE. J ) THEN
          RIJSQ = 0.d0
          DO IDIM = 1, DIM
            RXIJ = RXJ(IDIM) - RX(IDIM,TAU,K)
          C
            RXIJ = RXIJ -
            :   DNINT ( RXIJ/SIGM(IDIM) ) * SIGM(IDIM)
            C
            RIJSQ = RIJSQ + RXIJ * RXIJ
            C
            ENDDO

          C ** EUCLIDEAN DISTANCE
          RXIJ = COS(RXJ(1))*COS(RX(1,TAU,K))*
          :   COS(RXJ(2))*COS(RX(2,TAU,K))
          C
          RYIJ = COS(RXJ(1))*COS(RX(1,TAU,K))*
          :   SIN(RXJ(2))*SIN(RX(2,TAU,K))
          C
          RZIJ = SIN(RXJ(1))*SIN(RX(1,TAU,K))
          RIJSQ = RXIJ + RYIJ + RZIJ
          RIJSQ = RADIUS**2*(2*(1.-RIJSQ))

          CALL POT (RIJSQ, VIJ, WIJ, POTK)
          V = V + VIJ
          W = W + WIJ
        C
        ENDDIF
      C
      ENDDIF
    100 CONTINUE

    C
    RETURN

    V = V - LOG(ABS(RADIUS**2*COS(RXI(1))))/LS
    W = W - LOG(ABS(RADIUS**2*COS(RXI(1))))/LS

    IF (I.NE. J) THEN
      DO IDIM = 1, DIM
        RXIJ = RXI(IDIM) - RXJ(IDIM)
      C
        RXIJ = RXIJ -
        :   DNINT ( RXIJ/SIGM(IDIM) ) * SIGM(IDIM)
        C
        RIJSQ = RIJSQ + RXIJ * RXIJ
        C
        ENDDO

      C ** EUCLIDEAN DISTANCE
      RXIJ = COS(RXI(1))*COS(RXJ(1))*
      :   COS(RXI(2))*COS(RXJ(2))
      C
    C
    ENDDIF
  
```

```

100 CONTINUE

C RETURN

V = V - LOG(ABS(RADIUS**2*COS(RXI(1))))/LS
W = W - LOG(ABS(RADIUS**2*COS(RXI(1))))/LS

IF (I.NE. J) THEN
  RIJSQ = 0.d0
  DO IDIM = 1, DIM
    RXIJ = RXI(IDIM) - RXJ(IDIM)

    RXIJ = RXIJ -
      : DWINT ( RXIJ/SIGM(IDIM) )*SIGM(IDIM)
    RIJSQ = RIJSQ + RXIJ * RXIJ
  ENDDO

C ** EUCLIDEAN DISTANCE
  RXIJ = COS(RXI(1))*COS(RXJ(1))*
  : COS(RXI(2))*COS(RXJ(2))
  RYIJ = COS(RXI(1))*COS(RXJ(1))*
  : SIN(RXI(2))*SIN(RXJ(2))
  RZIJ = SIN(RXI(1))*SIN(RXJ(1))
  RIJSQ = RXIJ + RYIJ + RZIJ
  RIJSQ = RADIUS**2*(2*(1.-RIJSQ))

  CALL POT (RIJSQ, VIJ, WIJ, POTK)
  V = V + VIJ
  W = W + WIJ
  V = V - LOG(ABS(RADIUS**2*COS(RXJ(1))))/LS
  W = W - LOG(ABS(RADIUS**2*COS(RXJ(1))))/LS
ENDIF

RETURN
END

SUBROUTINE KENERGY ( RXI, I, TAU, KE )
  IMPLICIT NONE
C *****
C ** RETURNS THE KINETIC ENERGY OF ATOM I WITH ALL OTHER ATOMS. **
C **
C ** PRINCIPAL VARIABLES: **
C **
C ** INTEGER I THE ATOM OF INTEREST **
C ** INTEGER NP THE NUMBER OF ATOMS **
C ** INTEGER TAU THE TIMESTEP **
C ** REAL*8 RX, RY, RZ THE ATOM POSITIONS **
C ** REAL*8 RXI,RYI,RZI THE COORDINATES OF ATOM I **
C ** REAL*8 KE THE KINETIC ENERGY OF ATOM I **
C **
C ** USAGE: **
C **
C ** THIS SUBROUTINE IS USED TO CALCULATE THE CHANGE OF ENERGY **
C ** DURING A TRIAL MOVE OF ATOM I. IT IS CALLED BEFORE AND **
C ** AFTER THE RANDOM DISPLACEMENT OF I. **
C *****
  INCLUDE 'mc-sph.par'

  REAL*8 RXI(MDIM), KE
  REAL*8 RXIP1, RXIS1, RXIP2, RXIS2, RXII
  INTEGER*8 I, TAU, IDIM

  KE = 0.d0

  RXIP1 = RX(1,TAU-1,I)
  RXIS1 = RX(1,TAU+1,I)
  RXII = RXI(1) - RXIP1
  RXII = RXII - DWINT ( RXII/SIGM(1) )*SIGM(1)
  KE=KE+0.5*FTM*(RADIUS*RXII/LS)**2.
  RXII = RXI(1) - RXIS1
  RXII = RXII - DWINT ( RXII/SIGM(1) )*SIGM(1)
  KE=KE+0.5*FTM*(RADIUS*RXII/LS)**2.

  RXIP2 = RX(2,TAU-1,I)
  RXIS2 = RX(2,TAU+1,I)
  RXII = RXI(2) - RXIP2
  RXII = RXII - DWINT ( RXII/SIGM(2) )*SIGM(2)
  KE=KE+0.5*FTM*(RADIUS*COS(RXIP1)*RXII/LS)**2.
  RXII = RXI(2) - RXIS2
  RXII = RXII - DWINT ( RXII/SIGM(2) )*SIGM(2)
  KE=KE+0.5*FTM*(RADIUS*COS(RXI(1))*RXII/LS)**2.

  RETURN
END

SUBROUTINE KENERGY ( RXI, IP, TAU, KE )
  IMPLICIT NONE
C *****
C ** RETURNS THE KINETIC ENERGY OF ATOM I WITH ALL OTHER ATOMS. **
C **
C ** PRINCIPAL VARIABLES: **
C **
C ** INTEGER I THE ATOM OF INTEREST **
C ** INTEGER NP THE NUMBER OF ATOMS **
C ** INTEGER TAU THE TIMESTEP **
C ** REAL*8 RX, RY, RZ THE ATOM POSITIONS **
C ** REAL*8 RXI,RYI,RZI THE COORDINATES OF ATOM I **
C ** REAL*8 KE THE KINETIC ENERGY OF ATOM I **
C **
C ** USAGE: **
C **
C ** THIS SUBROUTINE IS USED TO CALCULATE THE CHANGE OF ENERGY **
C ** DURING A TRIAL MOVE OF ATOM I. IT IS CALLED BEFORE AND **
C ** AFTER THE RANDOM DISPLACEMENT OF I. **
C *****
  INCLUDE 'mc-sph.par'

  REAL*8 RXI(MDIM), KE
  REAL*8 RXIS, RXII

  INTEGER*8 IP, TAU, IDIM

  KE = 0.d0

  RXIS = RX(1,TAU+1,IP)
  RXII = RXI(1) - RXIS
  RXII = RXII - DWINT ( RXII/SIGM(1) )*SIGM(1)
  KE=KE+0.5*FTM*(RADIUS*RXII/LS)**2.

  RXIS = RX(2,TAU+1,IP)
  RXII = RXI(2) - RXIS
  RXII = RXII - DWINT ( RXII/SIGM(2) )*SIGM(2)
  KE=KE+0.5*FTM*(RADIUS*RXII/LS)**2.

  RETURN
END

SUBROUTINE KWIND ( WIND )
  IMPLICIT NONE
C *****
C ** RETURNS THE WINDING NUMBER. **
C *****
  INCLUDE 'mc-sph.par'

  REAL*8 WIND, WI, SURF
  REAL*8 RX11, RX21, RX31, RX12, RX22, RX32
  INTEGER*8 I, J, IDIM

  WIND = 0.d0
  SURF = 4*PI*RADIUS**2
  DO I = 1, NP
    DO J = 1, FTNO - 1
      RX11 = RX(1,J ,I)
      RX21 = RX(1,J+1,I)
      RX31 = RX(1,J+2,I)
      RX12 = RX(2,J ,I)
      RX22 = RX(2,J+1,I)
      RX32 = RX(2,J+2,I)
      WI = ((RX21-RX11)*(RX32-RX22)-(RX22-RX12)*(RX31-RX21))*
      : RADIUS**2*COS(RX21)
      WIND = WIND + WI
    ENDDO
  ENDDO
  IF (WIND.GT.SURF) WIND = SURF
  WIND = WIND**2

20 CONTINUE
  RETURN
END

REAL*8 FUNCTION RANF ( DUMMY )
  IMPLICIT NONE
C *****
C ** RETURNS A UNIFORM RANDOM VARIATE IN THE RANGE 0 TO 1. **
C **
C ** ** WARNING ** **
C ** ** ** ** **
C ** GOOD RANDOM NUMBER GENERATORS ARE MACHINE SPECIFIC. **
C ** PLEASE USE THE ONE RECOMMENDED FOR YOUR MACHINE. **
C **
C ** RAND(FLAG) returns a pseudo-random number from a uniform **
C ** distribution between 0 and 1. If FLAG is 0, the next number **
C ** in the current sequence is returned; if FLAG is 1, the **
C ** generator is restarted by CALL SRAND(0); if FLAG has any **
C ** other value, it is used as a new seed with SRAND. **
C *****
  INTEGER*8 L, C, M
  PARAMETER ( L = 1029, C = 221591, M = 1048576 )
  INTEGER*8 SEED
  SAVE SEED
  DATA SEED / 0 /
  REAL*8 DUMMY

  SEED = MOD ( SEED * L + C, M )
  RANF = DBLE( SEED ) / M

  RANF = RAND ( )

  RETURN
END

SUBROUTINE READCN ( CNFILE )
  IMPLICIT NONE
C *****
C ** SUBROUTINE TO READ IN THE CONFIGURATION FROM UNIT 10 **
C *****
  INCLUDE 'mc-sph.par'

  CHARACTER CNFILE(*), HASH*1, MYFMT*77
  INTEGER*8 CNUNIT, I, J, NNP, NI, IDIM
  PARAMETER ( CNUNIT = 10 )

C *****
  OPEN ( UNIT = CNUNIT, FILE = CNFILE, STATUS = 'OLD' )
  WRITE(MYFMT,'(A,I10,A)') '(I3,3X',DIM,'(F12.6,3X))'

  READ ( CNUNIT,* ) HASH, FTNO, NNP
  IF ( NNP.NE. NP ) STOP 'N ERROR IN READCN'

  DO 100 I = 1, NNP
    READ ( CNUNIT,* ) HASH, NEXT(I)
    NI = NEXT(I)
    DO 90 J = 1, FTNO+1
      READ ( CNUNIT, MYFMT) LEXT(I), (RX(IDIM,J,I),IDIM=1,DIM)
    END DO
  END DO

```



```

      RXIJ = COS(RX(1,TAU,I))*COS(RX(1,TAU,J))*
:      COS(RX(2,TAU,I))*COS(RX(2,TAU,J))
      RYIJ = COS(RX(1,TAU,I))*COS(RX(1,TAU,J))*
:      SIN(RX(2,TAU,I))*SIN(RX(2,TAU,J))
      RZIJ = SIN(RX(1,TAU,I))*SIN(RX(1,TAU,J))
      RIJSQ = RXIJ + RYIJ + RZIJ
c      RIJ = 2*RADIUS*SIN(ACOS(RIJSQ)/2.)
      RIJ = RADIUS*SQRT(2.-2*RIJSQ)

C      Geodesic Distance
      RIJ = RADIUS*ACOS(SIN(RX(1,TAU,I))*SIN(RX(1,TAU,J))+
c      : COS(RX(1,TAU,I))*COS(RX(1,TAU,J))*COS(RX(2,TAU,I)-RX(2,TAU,J)))

      BIN = INT ( RIJ/DELR ) + 1

      IF (BIN .LE. MAXBIN) THEN
        HIST(BIN) = HIST(BIN) + 2
      ENDIF

      ENDDO
    ENDDO

      RETURN
    END

      SUBROUTINE MAPPINGD()
      IMPLICIT NONE
C      *****
C      ** CHANGE COORDINATES (DIRECT) **
C      *****
      INCLUDE 'mc-sph.par'

      INTEGER*8 I,J

      DO I=1,NP
        DO J=0,FTNO+1
          RP(1,J,I)=RX(1,J,I)
          RP(2,J,I)=RX(2,J,I)
        ENDDO
      ENDDO

      RETURN
    END

      SUBROUTINE MAPPINGI()
      IMPLICIT NONE
C      *****
C      ** CHANGE COORDINATES (INVERSE) **
C      *****
      INCLUDE 'mc-sph.par'

      INTEGER*8 I,J

      DO I=1,NP
        DO J=0,FTNO+1
          RX(1,J,I)=RP(1,J,I)
          RX(2,J,I)=RP(2,J,I)
        ENDDO
      ENDDO

      RETURN
    END

      SUBROUTINE GAUSS(CP,GA)
      IMPLICIT NONE
C      *****
C      ** GAUSSIAN TRANSITION PROBABILITY FOR BROWNIAN BRIDGE **
C      *****
      INCLUDE 'mc-sph.par'

      INTEGER*8 I,J,K,CP,MCM
      REAL*8 GA,VAR,DD

      MCM = CP+MBM-FLOOR((CP+MBM-.1)/FTNO)*FTNO
      VAR = 2*LS/FTM

      GA = 0.DO
      DO I=1,DIM
        DO J=1,NP
          IF(CP+MBM.LE.FTNO)THEN
            DO K=CP+1,MCM
              DD=RPN(I,K,J)-RPN(I,K-1,J)
              DD=DD-DNINT ( DD/SIGM(I) )*SIGM(I)
              GA=GA+DD**2
              DD=RP(I,K,J)-RP(I,K-1,J)
              DD=DD-DNINT ( DD/SIGM(I) )*SIGM(I)
              GA=GA+DD**2
            ENDDO
          ELSE
            DO K=CP+1,FTNO
              DD=RPN(I,K,J)-RPN(I,K-1,J)
              DD=DD-DNINT ( DD/SIGM(I) )*SIGM(I)
              GA=GA+DD**2
              DD=RP(I,K,J)-RP(I,K-1,J)
              DD=DD-DNINT ( DD/SIGM(I) )*SIGM(I)
              GA=GA+DD**2
            ENDDO
          DO K=1,MCM
            DD=RPN(I,K,J)-RPN(I,K-1,J)
            DD=DD-DNINT ( DD/SIGM(I) )*SIGM(I)
            GA=GA+DD**2
            DD=RP(I,K,J)-RP(I,K-1,J)
            DD=DD-DNINT ( DD/SIGM(I) )*SIGM(I)
            GA=GA+DD**2
          ENDDO
        ENDDIF
      ENDDO
    ENDDO
  
```

```

      GA = EXP(GA/VAR)

      RETURN
    END

      SUBROUTINE EQUIV(A,B)
      IMPLICIT NONE
C      *****
C      ** A = B WITH A, B TWO PATHS **
C      *****
      INCLUDE 'mc-sph.par'

      INTEGER*8 I,J,K
      REAL*8 A(MDIM,0:N,MNP),B(MDIM,0:N,MNP)

      DO I=1,DIM
        DO J=0,FTNO+1
          DO K=1,NP
            A(I,J,K)=B(I,J,K)
          ENDDO
        ENDDO
      ENDDO

      RETURN
    END

      *****
      *** mc-sph.par *****
      *****

      REAL*8 PI
      REAL*8 DELR
      INTEGER*8 MDIM, N, MNP

      PARAMETER ( PI = 3.14159265358979323846264338328d0 )

      PARAMETER ( MDIM = 10 ) ! maximum number of dimensions
      PARAMETER ( MNP = 1000 ) ! maximum number of particles
      PARAMETER ( N = 3000 ) ! maximum number of time slices
      PARAMETER ( DELR = 0.01d0 ) ! grid spacing for g(r)

      INTEGER*8 DIM
      REAL*8 RX(MDIM,0:N,MNP)
      REAL*8 RPN(MDIM,0:N,MNP),RP(MDIM,0:N,MNP)
      REAL*8 FTM, LS, SIGMA, SIGM(MDIM), RADIUS
      REAL*8 SIG, EPSA, EPSR, EPS, RCUT
      INTEGER*8 FTNO, NP
      INTEGER*8 NEXT(MNP), LEXT(MNP), MEXT(N,MNP), MBM

      ! path
      COMMON / BLOCK1 / RX, RP, RPN, DIM
      ! pair-potential parameters
      COMMON / BLOCK2 / SIG, EPSR, EPSA, EPS, RCUT
      ! mass, timestep, box edge, # timeslices, # particles, radius
      COMMON / BLOCK3 / FTM, LS, SIGMA, SIGM, FTNO, NP, RADIUS
      ! permutations
      COMMON / BLOCK4 / NEXT, LEXT, MEXT, MBM

      *****
      *** data-gr-rs.in *****
      *****

      0 number of spatial dimensions (2 sphere)
      2
      1 seed of the random sequence RAND
      3
      2 if bose (T/F)
      T
      3 number of particles (<= MNP)
      10
      4 the potential SUBROUTINE POT
      FREE
      5 # time slices = 1/temperature/timestep (< N)
      50
      6 mass (hbar = kb = 1)
      1.d0
      7 # of cycles (nstep)
      5000000000000000000
      8 # of steps between output lines (iprint)
      100
      9 # of steps between configuration saves (isave)
      100
      10 # of steps for equilibration (iequi)
      100
      11 # of steps for acceptance ratios (iratio)
      100
      12 # of steps for rdf calculation (icalcg < #5)
      10
      13 configuration file name
      conf.xyz
      14 0 init zero, 1 init, 2 rest conf, 3 rest full
      1
      15 radius of the sphere
      5.d0
      16 temperature THERMODYNAMICS
      .03d0
      17 maximum displacement/box edge
      .05d0
      18 maximum # of bridge timeslices (> 1; <= #5)
      10
      19 potential cutoff distance (LJ) SUBROUTINE POT
      2.d0
      20 sig (LJ 2.566) SUBROUTINE POT
      1.d0
      21 epsr (LJ INIT) SUBROUTINE POT
      1.d10
      22 epsa SUBROUTINE POT
      1.d0
      23 eps (LJ 10.22) SUBROUTINE POT
  
```

1.d1
24 if only displace (T/F)
F
25 if only bridge (T/F)
F

AUTHOR DECLARATIONS

Conflicts of interest

None declared.

Data availability

The data that support the findings of this study are available from the corresponding author upon reasonable request.

Funding

None declared.

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